

Rational Exponents

SWBAT simplify rational exponents by converting them into radicals.

Rational Exponent: _____

- We can rewrite expressions with rational exponents as radical expressions to help us evaluate them more easily
- The denominator of the fraction is the index (root) of your radical and the numerator is the power of the base inside the radical
- **Example:** $x^{\frac{a}{b}} = \sqrt[b]{x^a}$

****Fill out the chart below to refresh on our squares and cubes!****

	1	2	3	4	5	6	7	8	9	10
Squared										
Cubed										

Example 1: Simplify each expression

*Turn it into a radical. The numerator is the power of the base, and the denominator is the number in the corner of the radical!

a) $27^{\frac{1}{3}}$

a) $a^{\frac{1}{6}}$

b) $64^{\frac{1}{2}}$

b) $m^{\frac{1}{2}}$

c) $8^{\frac{2}{3}}$

c) $x^{\frac{3}{4}}$

Example 2: Write each expression as a Rational Exponent

*The numerator is the power of the base, and the denominator is the number in the corner of the square root sign!

a) $\sqrt{x^3}$

a) $\sqrt[3]{m}$

b) $\sqrt{5y}$

b) $\sqrt[3]{2y^2}$

c) $(\sqrt[4]{b})^3$

c) $\sqrt{-6}$

Product of powers: Keep the _____ the same and _____ the exponents.

a) $(-5)^{\frac{1}{3}} \cdot (-5)^{\frac{1}{3}} \cdot (-5)^{\frac{1}{3}}$

b) $7^{\frac{1}{2}} \cdot 7^{\frac{1}{2}}$

c) $x^{\frac{1}{4}} \cdot x^{\frac{2}{4}}$

Power of a power: Keep the _____ the same and _____ the exponents.

a) $4(a^{\frac{1}{2}})^6$

b) $(3x^{\frac{1}{3}})^3$

c) $(16x^6y^{-1})^{\frac{1}{2}}$

Rational Exponents

Name: _____

Classwork

Directions: Evaluate each expression; resulting answers should not contain any radicals:

1) $5^2\left(\frac{1}{5}\right)^3$

2) $\frac{3}{3^{-2}}$

3) $\sqrt[4]{16}$

4) $\sqrt[5]{\frac{1}{32}}$

5) $4^{\frac{3}{2}} \times 4^{\frac{3}{2}}$

6) $\frac{\sqrt[3]{-3}}{\sqrt[3]{96}}$

7) $8^{\frac{2}{3}} 8^{\frac{1}{3}}$

8) $\sqrt[3]{5^3}$

9) $\sqrt[8]{6^8}$

Directions: Simplify the expressions. Write answers as a rational exponent (if needed).

1) $\sqrt[4]{z^{20}}$

2) $\sqrt[3]{x^4}$

3) $\sqrt[3]{c^3}$

4) $\sqrt[4]{256x^8}$

5) $\sqrt[4]{16y^{16}}$

6) $\sqrt[4]{16x^4z^8}$

7) $(\sqrt{x})(\sqrt{x})$

8) $(\sqrt[5]{x^7y})(\sqrt[5]{x^3y})$

9) $\sqrt[4]{81x^8y^4}$

Directions: Simplify the expression and eliminate any negative exponent(s):

1) $(2x^{\frac{3}{2}})(4x)^{\frac{1}{2}}$

2) $(-2a^{\frac{3}{4}})(5a^{\frac{3}{2}})$

3) $(8x^6)^{-\frac{2}{3}}$

4) $\left(\frac{-2x^{\frac{1}{3}}}{y^{\frac{1}{2}}z^{\frac{1}{6}}}\right)^6$

5) $\frac{(y^{10}z^{-5})^{\frac{1}{5}}}{(y^{-2}z^3)^{\frac{1}{3}}}$

6) $(x^{-5}y^3z^{10})^{-\frac{3}{5}}$

Rational Exponents

SWBAT simplify rational exponents by converting them into radicals.

Rational Exponent: Exponents in fraction form

- We can rewrite expressions with rational exponents as radical expressions to help us evaluate them more easily
- The denominator of the fraction is the index (root) of your radical and the numerator is the power of the base inside the radical

• Example: $x^{\frac{a}{b}} = \sqrt[b]{x^a}$

$$\times \begin{array}{l} \frac{a}{b} \rightarrow \text{power} \\ \quad \quad \rightarrow \text{root} \end{array}$$

Fill out the chart below to refresh on our squares and cubes!

	1	2	3	4	5	6	7	8	9	10
Squared	1	4	9	16	25	36	49	64	81	100
Cubed	1	8	27	64	125	216	343	512	729	1,000

Example 1: Simplify each expression

*Turn it into a radical. The numerator is the power of the base, and the denominator is the number in the corner of the radical!

a) $27^{\frac{1}{3}} = \sqrt[3]{27} = 3$ a) $a^{\frac{1}{6}} = \sqrt[6]{a}$

b) $64^{\frac{1}{2}} = \sqrt{64} = 8$ b) $m^{\frac{1}{2}} = \sqrt{m}$

c) $8^{\frac{2}{3}} = \sqrt[3]{8^2}$ c) $x^{\frac{3}{4}} = \sqrt[4]{x^3}$

Example 2: Write each expression as a Rational Exponent

*The numerator is the power of the base, and the denominator is the number in the corner of the square root sign!

a) $\sqrt{x^3} = x^{\frac{3}{2}}$ a) $\sqrt[3]{m} = m^{\frac{1}{3}}$

b) $\sqrt{5y} = (5y)^{\frac{1}{2}}$ b) $\sqrt[3]{2y^2} = (2)^{\frac{1}{3}} y^{\frac{2}{3}}$

c) $(\sqrt[4]{b})^3 = (b^{\frac{1}{4}})^3 = b^{\frac{3}{4}}$ c) $\sqrt{-6} = (-6)^{\frac{1}{2}}$

Product of powers: Keep the BASE the same and ADD the exponents.

a) $(-5)^{\frac{1}{3}} \cdot (-5)^{\frac{1}{3}} \cdot (-5)^{\frac{1}{3}}$

$$-5^{\frac{3}{3}} = (-5)$$

b) $7^{\frac{1}{2}} \cdot 7^{\frac{1}{2}}$

$$7^{\frac{2}{2}} = 7$$

c) $x^{\frac{1}{4}} \cdot x^{\frac{2}{4}}$

$$x^{\frac{3}{4}}$$

Power of a power: Keep the BASE the same and MULTIPLY the exponents.

a) $4(a^2)^6$

$$4a^{\frac{6}{2}} = 4a^3$$

b) $(3x^3)^{\frac{1}{3}}$

$$3^3 x^{\frac{3}{3}} = 27x$$

c) $(16x^6y^{-4})^{\frac{1}{2}}$

$$16^{\frac{1}{2}} x^{\frac{6}{2}} y^{\frac{-4}{2}} = \frac{4x^3}{y^2}$$

Rational Exponents

Classwork - DO ODD PROBLEMS!

Name: Key

Directions: Evaluate each expression; resulting answers should not contain any radicals:

- 1) $5^2 \left(\frac{1}{5}\right)^3 = 25 \left(\frac{1}{125}\right) = \frac{1}{5}$ or 2
 2) $\frac{3}{3^{-2}} = 3 \cdot 3^2 = 3 \cdot 9 = 27$
 $\sqrt[4]{16} = 2$
 4) $\sqrt[5]{\frac{1}{32}} = \left(\frac{1}{32}\right)^{\frac{1}{5}} = \frac{1}{2}$
 5) $4^{\frac{3}{2}} \times 4^{\frac{3}{2}} = 4^{\frac{6}{2}} = 4^3 = 64$
 $\frac{\sqrt{-3}}{\sqrt[3]{96}} = \frac{-3^{\frac{1}{2}}}{96^{\frac{1}{3}}} = -5$
 7) $8^{\frac{2}{3}} 8^{\frac{1}{3}} = 8^{\frac{3}{3}} = 8$
 8) $\sqrt[3]{5^3} = 5$
 9) $\sqrt[3]{6^8} = 6^{\frac{8}{3}}$

Directions: Simplify the expressions. Write answers as a rational exponent (if needed).

- 1) $\sqrt[4]{z^{20}} = z^{\frac{20}{4}} = z^5$
 2) $\sqrt[3]{x^4} = x^{\frac{4}{3}}$
 3) $\sqrt[3]{c^3} = c$
 4) $\sqrt[4]{256x^8} = 256^{\frac{1}{4}} x^{\frac{8}{4}} = 4x^2$
 5) $\sqrt[4]{16y^{16}} = 16^{\frac{1}{4}} y^{\frac{16}{4}} = 2y^4$
 6) $\sqrt[4]{16x^4z^8} = 2x z^2$
 7) $(\sqrt{x})(\sqrt{x}) = x$
 8) $(\sqrt[3]{x^7y})(\sqrt[3]{x^3y}) = x^{\frac{7}{3} + \frac{3}{3}} y^{\frac{1}{3} + \frac{1}{3}} = x^{\frac{10}{3}} y^{\frac{2}{3}}$
 9) $\sqrt[4]{81x^8y^4} = 3x^2y$

Directions: Simplify the expression and eliminate any negative exponent(s):

- 1) $(2x^{\frac{3}{2}})(4x)^{\frac{1}{2}} = 2x^{\frac{3}{2}} \cdot \frac{1}{2} x^{\frac{1}{2}} = x^{\frac{3}{2} + \frac{1}{2}} = x^2$
 2) $(-2a^{\frac{3}{4}})(5a^{\frac{3}{2}}) = -2a^{\frac{3}{4}} \cdot 5a^{\frac{3}{2}} = -10a^{\frac{3}{4} + \frac{6}{4}} = -10a^{\frac{9}{4}}$
 3) $(8x^6)^{\frac{2}{3}} = 8^{\frac{2}{3}} x^{\frac{12}{3}} = \frac{4}{x^4}$
 4) $\frac{(-2x^{\frac{1}{3}})^6}{y^{\frac{1}{2}}z^{\frac{1}{6}}} = \frac{-2^6 x^2}{y^{\frac{1}{2}}z^{\frac{1}{6}}} = \frac{64x^2}{y^{\frac{1}{2}}z^{\frac{1}{6}}}$
 5) $\frac{(y^{10}z^{-5})^{\frac{1}{5}}}{(y^{-2}z^3)^{\frac{1}{3}}} = \frac{y^{\frac{10}{5}}z^{-\frac{5}{5}}}{y^{-\frac{2}{3}}z^{\frac{3}{3}}} = \frac{y^2z^{-1}}{y^{-\frac{2}{3}}z^1} = \frac{y^2z^{-1} \cdot y^{\frac{2}{3}}z^{-1}}{z^1} = \frac{y^{\frac{8}{3}}z^{-2}}{z^1} = \frac{y^{\frac{8}{3}}}{z^3}$
 6) $(x^{-5}y^3z^{10})^{\frac{3}{5}} = x^{-3}y^{\frac{9}{5}}z^{\frac{30}{5}} = \frac{x^3 y^{\frac{9}{5}} z^6}{x^{-15} z^6}$